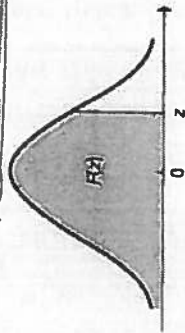


# APPENDIX TABLES

Table 1 Cumulative Distribution Function of the Standard Normal Distribution



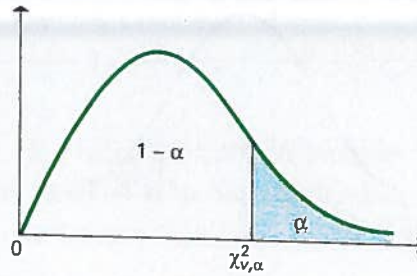
| z   | F(z)  | z   | F(z)  | z    | F(z)  | z    | F(z)  | z    | F(z)  |
|-----|-------|-----|-------|------|-------|------|-------|------|-------|
| .00 | .5000 | .91 | .8186 | 1.21 | .8869 | 1.51 | .9345 | 1.81 | .9649 |
| .01 | .5040 | .92 | .8212 | 1.22 | .8888 | 1.52 | .9357 | 1.82 | .9656 |
| .02 | .5080 | .93 | .8238 | 1.23 | .8907 | 1.53 | .9370 | 1.83 | .9664 |
| .03 | .5120 | .94 | .8264 | 1.24 | .8925 | 1.54 | .9382 | 1.84 | .9671 |
| .04 | .5160 | .95 | .8289 | 1.25 | .8944 | 1.55 | .9394 | 1.85 | .9678 |
| .05 | .5199 | .96 | .8315 | 1.26 | .8962 | 1.56 | .9406 | 1.86 | .9686 |
| .06 | .5239 | .97 | .8340 | 1.27 | .8980 | 1.57 | .9418 | 1.87 | .9693 |
| .07 | .5279 | .98 | .8365 | 1.28 | .8997 | 1.58 | .9429 | 1.88 | .9699 |
| .08 | .5319 | .99 | .8389 | 1.29 | .9015 | 1.59 | .9441 | 1.89 | .9706 |
| .09 | .5359 | .00 | .8413 | 1.30 | .9032 | 1.60 | .9452 | 1.90 | .9713 |
| .10 | .5398 | .01 | .8438 | 1.31 | .9049 | 1.61 | .9463 | 1.91 | .9719 |
| .11 | .5438 | .02 | .8461 | 1.32 | .9066 | 1.62 | .9474 | 1.92 | .9726 |
| .12 | .5478 | .03 | .8485 | 1.33 | .9082 | 1.63 | .9484 | 1.93 | .9732 |
| .13 | .5517 | .04 | .8508 | 1.34 | .9099 | 1.64 | .9495 | 1.94 | .9738 |
| .14 | .5557 | .05 | .8531 | 1.35 | .9115 | 1.65 | .9505 | 1.95 | .9744 |
| .15 | .5596 | .06 | .8554 | 1.36 | .9131 | 1.66 | .9515 | 1.96 | .9750 |
| .16 | .5636 | .07 | .8577 | 1.37 | .9147 | 1.67 | .9525 | 1.97 | .9756 |
| .17 | .5675 | .08 | .8599 | 1.38 | .9162 | 1.68 | .9535 | 1.98 | .9761 |
| .18 | .5714 | .09 | .8621 | 1.39 | .9177 | 1.69 | .9545 | 1.99 | .9767 |
| .19 | .5753 | .10 | .8643 | 1.40 | .9192 | 1.70 | .9554 | 2.00 | .9772 |
| .20 | .5793 | .11 | .8665 | 1.41 | .9207 | 1.71 | .9564 | 2.01 | .9778 |
| .21 | .5832 | .12 | .8686 | 1.42 | .9222 | 1.72 | .9573 | 2.02 | .9783 |
| .22 | .5871 | .13 | .8708 | 1.43 | .9236 | 1.73 | .9582 | 2.03 | .9788 |
| .23 | .5910 | .14 | .8729 | 1.44 | .9251 | 1.74 | .9591 | 2.04 | .9793 |
| .24 | .5948 | .15 | .8749 | 1.45 | .9265 | 1.75 | .9599 | 2.05 | .9798 |
| .25 | .5987 | .16 | .8770 | 1.46 | .9279 | 1.76 | .9608 | 2.06 | .9803 |
| .26 | .6026 | .17 | .8790 | 1.47 | .9292 | 1.77 | .9616 | 2.07 | .9808 |
| .27 | .6064 | .18 | .8810 | 1.48 | .9306 | 1.78 | .9625 | 2.08 | .9812 |
| .28 | .6103 | .19 | .8830 | 1.49 | .9319 | 1.79 | .9633 | 2.09 | .9817 |
| .29 | .6141 | .20 | .8849 | 1.50 | .9332 | 1.80 | .9641 | 2.10 | .9821 |
| .30 | .6179 |     |       |      |       |      |       | 2.11 | .9826 |

Table 1 Cumulative Distribution Function of the Standard Normal Distribution Continue

| z    | F(z)  | z    | F(z)  | z    | F(z)  | z    | F(z)  | z    | F(z)  |
|------|-------|------|-------|------|-------|------|-------|------|-------|
| 1.81 | .9649 | 2.21 | .9864 | 2.61 | .9955 | 3.01 | .9987 | 3.41 | .9997 |
| 1.82 | .9656 | 2.22 | .9868 | 2.62 | .9956 | 3.02 | .9987 | 3.42 | .9997 |
| 1.83 | .9664 | 2.23 | .9871 | 2.63 | .9957 | 3.03 | .9988 | 3.43 | .9997 |
| 1.84 | .9671 | 2.24 | .9875 | 2.64 | .9959 | 3.04 | .9988 | 3.44 | .9997 |
| 1.85 | .9678 | 2.25 | .9878 | 2.65 | .9960 | 3.05 | .9989 | 3.45 | .9997 |
| 1.86 | .9686 | 2.26 | .9881 | 2.66 | .9961 | 3.06 | .9989 | 3.46 | .9997 |
| 1.87 | .9693 | 2.27 | .9884 | 2.67 | .9962 | 3.07 | .9989 | 3.47 | .9997 |
| 1.88 | .9699 | 2.28 | .9887 | 2.68 | .9963 | 3.08 | .9990 | 3.48 | .9997 |
| 1.89 | .9706 | 2.29 | .9890 | 2.69 | .9964 | 3.09 | .9990 | 3.49 | .9998 |
| 1.90 | .9713 | 2.30 | .9893 | 2.70 | .9965 | 3.10 | .9990 | 3.50 | .9998 |
| 1.91 | .9719 | 2.31 | .9896 | 2.71 | .9966 | 3.11 | .9991 | 3.51 | .9998 |
| 1.92 | .9726 | 2.32 | .9898 | 2.72 | .9967 | 3.12 | .9991 | 3.52 | .9998 |
| 1.93 | .9732 | 2.33 | .9901 | 2.73 | .9968 | 3.13 | .9991 | 3.53 | .9998 |
| 1.94 | .9738 | 2.34 | .9904 | 2.74 | .9969 | 3.14 | .9992 | 3.54 | .9998 |
| 1.95 | .9744 | 2.35 | .9906 | 2.75 | .9970 | 3.15 | .9992 | 3.55 | .9998 |
| 1.96 | .9750 | 2.36 | .9909 | 2.76 | .9971 | 3.16 | .9992 | 3.56 | .9998 |
| 1.97 | .9756 | 2.37 | .9911 | 2.77 | .9972 | 3.17 | .9992 | 3.57 | .9998 |
| 1.98 | .9761 | 2.38 | .9913 | 2.78 | .9973 | 3.18 | .9993 | 3.58 | .9998 |
| 1.99 | .9767 | 2.39 | .9916 | 2.79 | .9974 | 3.19 | .9993 | 3.59 | .9998 |
| 2.00 | .9772 | 2.40 | .9918 | 2.80 | .9974 | 3.20 | .9993 | 3.60 | .9998 |
| 2.01 | .9778 | 2.41 | .9920 | 2.81 | .9975 | 3.21 | .9993 | 3.61 | .9998 |
| 2.02 | .9783 | 2.42 | .9922 | 2.82 | .9976 | 3.22 | .9994 | 3.62 | .9999 |
| 2.03 | .9788 | 2.43 | .9925 | 2.83 | .9977 | 3.23 | .9994 | 3.63 | .9999 |
| 2.04 | .9793 | 2.44 | .9927 | 2.84 | .9977 | 3.24 | .9994 | 3.64 | .9999 |
| 2.05 | .9798 | 2.45 | .9929 | 2.85 | .9978 | 3.25 | .9994 | 3.65 | .9999 |
| 2.06 | .9803 | 2.46 | .9931 | 2.86 | .9979 | 3.26 | .9994 | 3.66 | .9999 |
| 2.07 | .9808 | 2.47 | .9932 | 2.87 | .9979 | 3.27 | .9995 | 3.67 | .9999 |
| 2.08 | .9812 | 2.48 | .9934 | 2.88 | .9980 | 3.28 | .9995 | 3.68 | .9999 |
| 2.09 | .9817 | 2.49 | .9936 | 2.89 | .9981 | 3.29 | .9995 | 3.69 | .9999 |
| 2.10 | .9821 | 2.50 | .9938 | 2.90 | .9981 | 3.30 | .9995 | 3.70 | .9999 |
| 2.11 | .9826 | 2.51 | .9940 | 2.91 | .9982 | 3.31 | .9995 | 3.71 | .9999 |
| 2.12 | .9830 | 2.52 | .9941 | 2.92 | .9982 | 3.32 | .9996 | 3.72 | .9999 |
| 2.13 | .9834 | 2.53 | .9943 | 2.93 | .9983 | 3.33 | .9996 | 3.73 | .9999 |
| 2.14 | .9838 | 2.54 | .9945 | 2.94 | .9984 | 3.34 | .9996 | 3.74 | .9999 |
| 2.15 | .9842 | 2.55 | .9946 | 2.95 | .9984 | 3.35 | .9996 | 3.75 | .9999 |
| 2.16 | .9846 | 2.56 | .9948 | 2.96 | .9985 | 3.36 | .9996 | 3.76 | .9999 |
| 2.17 | .9850 | 2.57 | .9949 | 2.97 | .9985 | 3.37 | .9996 | 3.77 | .9999 |
| 2.18 | .9854 | 2.58 | .9951 | 2.98 | .9986 | 3.38 | .9996 | 3.78 | .9999 |
| 2.19 | .9857 | 2.59 | .9952 | 2.99 | .9986 | 3.39 | .9997 | 3.79 | .9999 |
| 2.20 | .9861 | 2.60 | .9953 | 3.00 | .9986 | 3.40 | .9997 | 3.80 | .9999 |

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**Table 7** Cutoff Points of the Chi-Square Distribution Function

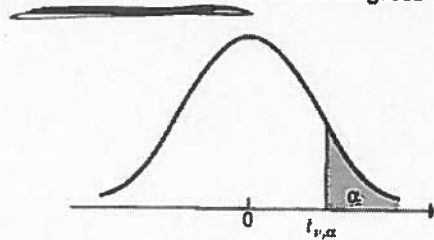


For selected probabilities  $\alpha$ , the table shows the values  $\chi^2_{v,\alpha}$  such that  $P(\chi^2_v > \chi^2_{v,\alpha}) = \alpha$ , where  $\chi^2_v$  is a chi-square random variable with  $v$  degrees of freedom. For example, the probability is .100 that a chi-square random variable with 10 degrees of freedom is greater than 15.99.

| v   | $\alpha$             |                      |                      |                      |        |       |       |       |       |       |
|-----|----------------------|----------------------|----------------------|----------------------|--------|-------|-------|-------|-------|-------|
|     | .995                 | .990                 | .975                 | .950                 | .900   | .100  | .050  | .025  | .010  | .005  |
| 1   | 0.0 <sup>4</sup> 393 | 0.0 <sup>3</sup> 157 | 0.0 <sup>3</sup> 982 | 0.0 <sup>2</sup> 393 | 0.0158 | 2.71  | 3.84  | 5.02  | 6.63  | 7.88  |
| 2   | 0.0100               | 0.0201               | 0.0506               | 0.103                | 0.211  | 4.61  | 5.99  | 7.38  | 9.21  | 10.60 |
| 3   | 0.072                | 0.115                | 0.216                | 0.352                | 0.584  | 6.25  | 7.81  | 9.35  | 11.34 | 12.84 |
| 4   | 0.207                | 0.297                | 0.484                | 0.711                | 1.064  | 7.78  | 9.49  | 11.14 | 13.28 | 14.86 |
| 5   | 0.412                | 0.554                | 0.831                | 1.145                | 1.61   | 9.24  | 11.07 | 12.83 | 15.09 | 16.75 |
| 6   | 0.676                | 0.872                | 1.24                 | 1.64                 | 2.20   | 10.64 | 12.59 | 14.45 | 16.81 | 18.55 |
| 7   | 0.989                | 1.24                 | 1.69                 | 2.17                 | 2.83   | 12.02 | 14.07 | 16.01 | 18.48 | 20.28 |
| 8   | 1.34                 | 1.65                 | 2.18                 | 2.73                 | 3.49   | 13.36 | 15.51 | 17.53 | 20.09 | 21.96 |
| 9   | 1.73                 | 2.09                 | 2.70                 | 3.33                 | 4.17   | 14.68 | 16.92 | 19.02 | 21.67 | 23.59 |
| 10  | 2.16                 | 2.56                 | 3.25                 | 3.94                 | 4.87   | 15.99 | 18.31 | 20.48 | 23.21 | 25.19 |
| 11  | 2.60                 | 3.05                 | 3.82                 | 4.57                 | 5.58   | 17.28 | 19.68 | 21.92 | 24.73 | 26.76 |
| 12  | 3.07                 | 3.57                 | 4.40                 | 5.23                 | 6.30   | 18.55 | 21.03 | 23.34 | 26.22 | 28.30 |
| 13  | 3.57                 | 4.11                 | 5.01                 | 5.89                 | 7.04   | 19.81 | 22.36 | 24.74 | 27.69 | 29.82 |
| 14  | 4.07                 | 4.66                 | 5.63                 | 6.57                 | 7.79   | 21.06 | 23.68 | 26.12 | 29.14 | 31.32 |
| 15  | 4.60                 | 5.23                 | 6.26                 | 7.26                 | 8.55   | 22.31 | 25.00 | 27.49 | 30.58 | 32.80 |
| 16  | 5.14                 | 5.81                 | 6.91                 | 7.96                 | 9.31   | 23.54 | 26.30 | 28.85 | 32.00 | 34.27 |
| 17  | 5.70                 | 6.41                 | 7.56                 | 8.67                 | 10.09  | 24.77 | 27.59 | 30.19 | 33.41 | 35.72 |
| 18  | 6.26                 | 7.01                 | 8.23                 | 9.39                 | 10.86  | 25.99 | 28.87 | 31.53 | 34.81 | 37.16 |
| 19  | 6.84                 | 7.63                 | 8.91                 | 10.12                | 11.65  | 27.20 | 30.14 | 32.85 | 36.19 | 38.58 |
| 20  | 7.43                 | 8.26                 | 9.59                 | 10.85                | 12.44  | 28.41 | 31.41 | 34.17 | 37.57 | 40.00 |
| 21  | 8.03                 | 8.90                 | 10.28                | 11.59                | 13.24  | 29.62 | 32.67 | 35.48 | 38.93 | 41.40 |
| 22  | 8.64                 | 9.54                 | 10.98                | 12.34                | 14.04  | 30.81 | 33.92 | 36.78 | 40.29 | 42.80 |
| 23  | 9.26                 | 10.20                | 11.69                | 13.09                | 14.85  | 32.01 | 35.17 | 38.08 | 41.64 | 44.18 |
| 24  | 9.89                 | 10.86                | 12.40                | 13.85                | 15.66  | 33.20 | 36.42 | 39.36 | 42.98 | 45.56 |
| 25  | 10.52                | 11.52                | 13.12                | 14.61                | 16.47  | 34.38 | 37.65 | 40.65 | 44.31 | 46.93 |
| 26  | 11.16                | 12.20                | 13.84                | 15.38                | 17.29  | 35.56 | 38.89 | 41.92 | 45.64 | 48.29 |
| 27  | 11.81                | 12.88                | 14.57                | 16.15                | 18.11  | 36.74 | 40.11 | 43.19 | 46.96 | 49.64 |
| 28  | 12.46                | 13.56                | 15.31                | 16.93                | 18.94  | 37.92 | 41.34 | 44.46 | 48.28 | 50.99 |
| 29  | 13.12                | 14.26                | 16.05                | 17.71                | 19.77  | 39.09 | 42.56 | 45.72 | 49.59 | 52.34 |
| 30  | 13.79                | 14.95                | 16.79                | 18.49                | 20.60  | 40.26 | 43.77 | 46.98 | 50.89 | 53.67 |
| 40  | 20.71                | 22.16                | 24.43                | 26.51                | 29.05  | 51.81 | 55.76 | 59.34 | 63.69 | 66.77 |
| 50  | 27.99                | 29.71                | 32.36                | 34.76                | 37.69  | 63.17 | 67.50 | 71.42 | 76.15 | 79.49 |
| 60  | 35.53                | 37.48                | 40.48                | 43.19                | 46.46  | 74.40 | 79.08 | 83.30 | 88.38 | 91.95 |
| 70  | 43.28                | 45.44                | 48.76                | 51.74                | 55.33  | 85.53 | 90.53 | 95.02 | 100.4 | 104.2 |
| 80  | 51.17                | 53.54                | 57.15                | 60.39                | 64.28  | 96.58 | 101.9 | 106.6 | 112.3 | 116.3 |
| 90  | 59.20                | 61.75                | 65.65                | 69.13                | 73.29  | 107.6 | 113.1 | 118.1 | 124.1 | 128.3 |
| 100 | 67.33                | 70.06                | 74.22                | 77.93                | 82.36  | 118.5 | 124.3 | 129.6 | 135.8 | 140.2 |

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**Table 8** Upper Critical Values of Student's  $t$  Distribution with  $\nu$  Degrees of Freedom



For selected probabilities,  $\alpha$ , the table shows the values  $t_{\nu, \alpha}$  such that  $P(t_{\nu} > t_{\nu, \alpha}) = \alpha$ , where  $t_{\nu}$  is a Student's  $t$  random variable with  $\nu$  degrees of freedom. For example, the probability is .10 that a Student's  $t$  random variable with 10 degrees of freedom exceeds 1.372.

| $\nu$    | PROBABILITY OF EXCEEDING THE CRITICAL VALUE |       |        |        |        |         |
|----------|---|-------|--------|--------|--------|---------|
|          | 0.10  | 0.05  | 0.025  | 0.01   | 0.005  | 0.001   |
| 1        | 3.078                                       | 6.314 | 12.706 | 31.821 | 63.657 | 318.313 |
| 2        | 1.886                                       | 2.920 | 4.303  | 6.965  | 9.925  | 22.327  |
| 3        | 1.638                                       | 2.353 | 3.182  | 4.541  | 5.841  | 10.215  |
| 4        | 1.533                                       | 2.132 | 2.776  | 3.747  | 4.604  | 7.173   |
| 5        | 1.476                                       | 2.015 | 2.571  | 3.365  | 4.032  | 5.893   |
| 6        | 1.440                                       | 1.943 | 2.447  | 3.143  | 3.707  | 5.208   |
| 7        | 1.415                                       | 1.895 | 2.365  | 2.998  | 3.499  | 4.782   |
| 8        | 1.397                                       | 1.860 | 2.306  | 2.896  | 3.355  | 4.499   |
| 9        | 1.383                                       | 1.833 | 2.262  | 2.821  | 3.250  | 4.296   |
| 10       | 1.372                                       | 1.812 | 2.228  | 2.764  | 3.169  | 4.143   |
| 11       | 1.363                                       | 1.796 | 2.201  | 2.718  | 3.106  | 4.024   |
| 12       | 1.356                                       | 1.782 | 2.179  | 2.681  | 3.055  | 3.929   |
| 13       | 1.350                                       | 1.771 | 2.160  | 2.650  | 3.012  | 3.852   |
| 14       | 1.345                                       | 1.761 | 2.145  | 2.624  | 2.977  | 3.787   |
| 15       | 1.341                                       | 1.753 | 2.131  | 2.602  | 2.947  | 3.733   |
| 16       | 1.337                                       | 1.746 | 2.120  | 2.583  | 2.921  | 3.686   |
| 17       | 1.333                                       | 1.740 | 2.110  | 2.567  | 2.898  | 3.646   |
| 18       | 1.330                                       | 1.734 | 2.101  | 2.552  | 2.878  | 3.610   |
| 19       | 1.328                                       | 1.729 | 2.093  | 2.539  | 2.861  | 3.579   |
| 20       | 1.325                                       | 1.725 | 2.086  | 2.528  | 2.845  | 3.552   |
| 21       | 1.323                                       | 1.721 | 2.080  | 2.518  | 2.831  | 3.527   |
| 22       | 1.321                                       | 1.717 | 2.074  | 2.508  | 2.819  | 3.505   |
| 23       | 1.319                                       | 1.714 | 2.069  | 2.500  | 2.807  | 3.485   |
| 24       | 1.318                                       | 1.711 | 2.064  | 2.492  | 2.797  | 3.467   |
| 25       | 1.316                                       | 1.708 | 2.060  | 2.485  | 2.787  | 3.450   |
| 26       | 1.315                                       | 1.706 | 2.056  | 2.479  | 2.779  | 3.435   |
| 27       | 1.314                                       | 1.703 | 2.052  | 2.473  | 2.771  | 3.421   |
| 28       | 1.313                                       | 1.701 | 2.048  | 2.467  | 2.763  | 3.408   |
| 29       | 1.311                                       | 1.699 | 2.045  | 2.462  | 2.756  | 3.396   |
| 30       | 1.310                                       | 1.697 | 2.042  | 2.457  | 2.750  | 3.385   |
| 40       | 1.303                                       | 1.684 | 2.021  | 2.423  | 2.704  | 3.307   |
| 60       | 1.296                                       | 1.671 | 2.000  | 2.390  | 2.660  | 3.232   |
| 100      | 1.290                                       | 1.660 | 1.984  | 2.364  | 2.626  | 3.174   |
| $\infty$ | 1.282                                       | 1.645 | 1.960  | 2.326  | 2.576  | 3.090   |

NIST/SEMATECH e-Handbook of Statistical Methods, <http://www.itl.nist.gov/div898/handbook/>, September 2011.